



Centre de Desenvolupament de Sensors, Instrumentació i Sistemes  
Departament d'Òptica i Optometria  
UNIVERSITAT POLITÈCNICA DE CATALUNYA

# *Curvature sensing: a new method for ocular wave- front determination*

F. Díaz-Doutón, S.O. Luque, V. Lapuente, M. Arjona, J. Pujol,  
F. Sanabria

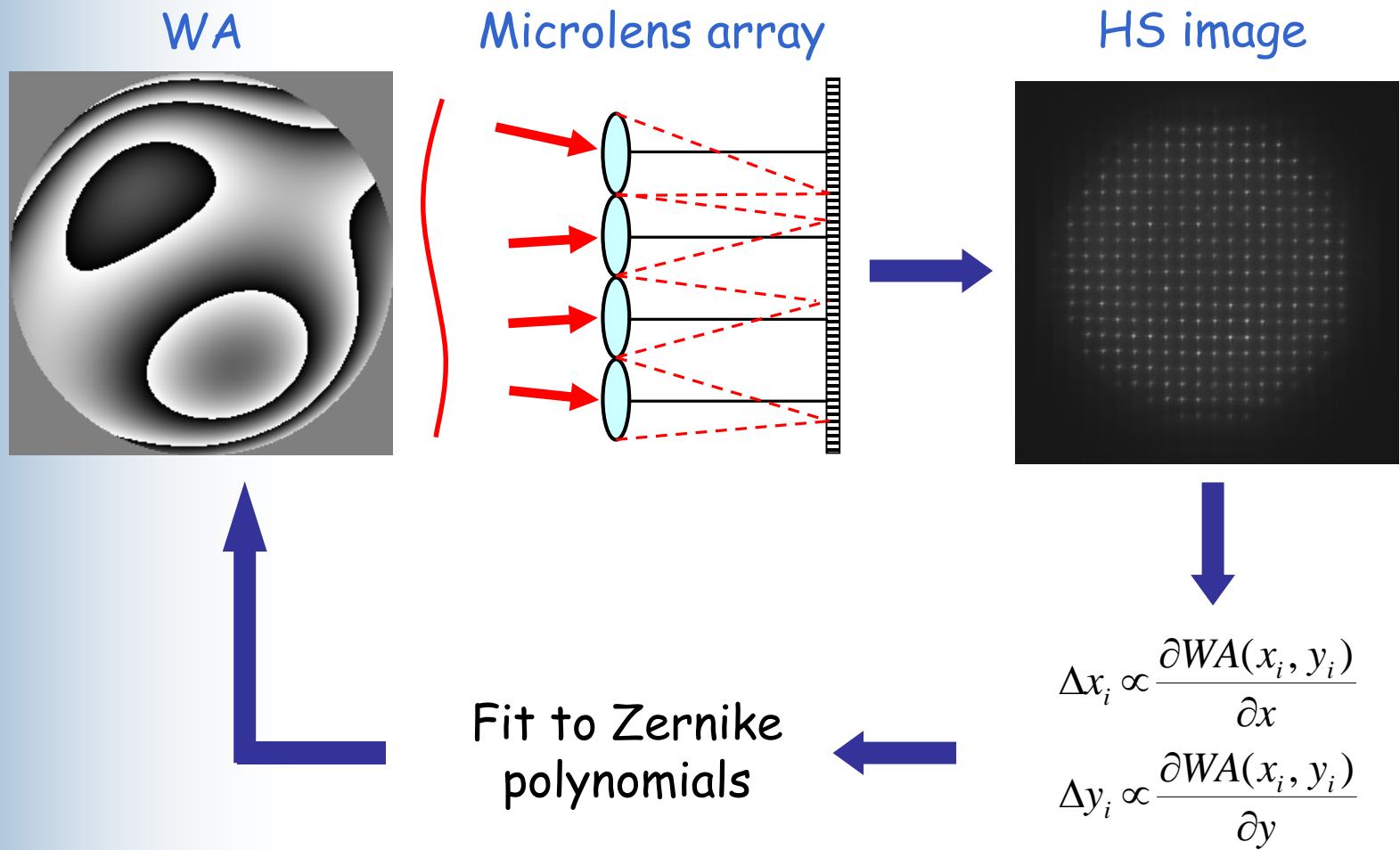
*3<sup>rd</sup> European Meeting in Physiological Optics*

London, september 2006

# Curvature sensing: a new method for ocular wave-front determination

Current ocular wave-front sensors are based on sampling the slope of the wave-front across the pupil

Example: Hartmann-Shack sensor



# DRAWBACK



*The number of samples limits the aberration order that can be achieved in the reconstruction !*

**Important when high order aberrations are significant\***

\* F. Diaz-Douton et al., "Comparison of the retinal image quality with a Hartmann-Shack sensor and a double-pass instrument", IOVS

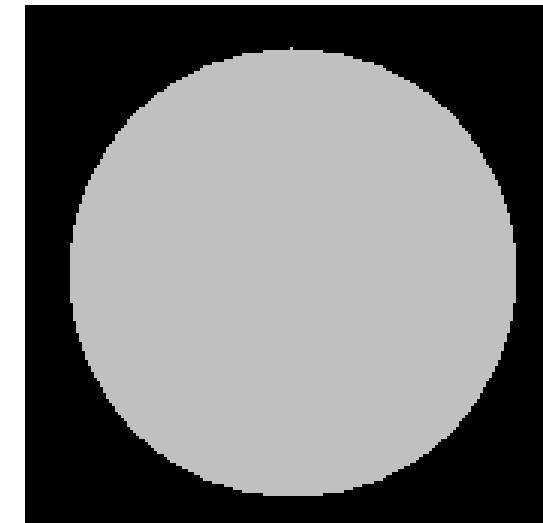
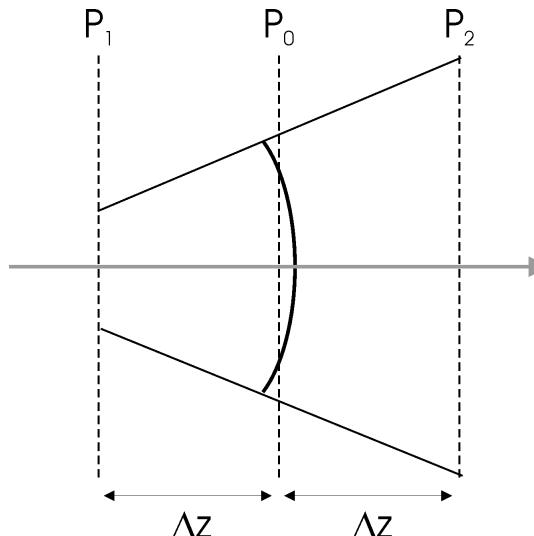
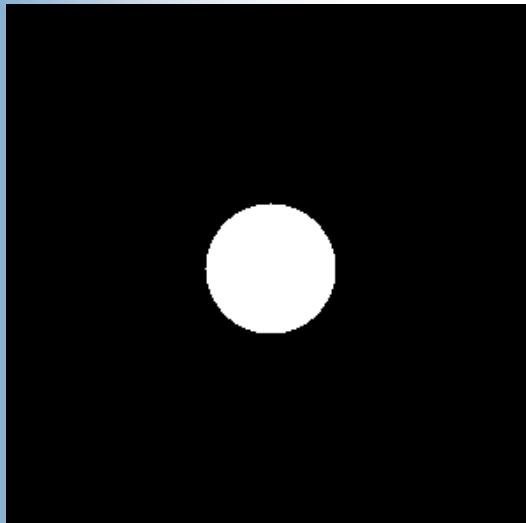
# Curvature sensing: a new method for ocular wave-front determination

## ALTERNATIVE



### Curvature sensor

Based on the changes in light intensity as it travels through its optical path



## Irradiance Transport Equation:

$$k \frac{\partial}{\partial z} I(r, z) = -\nabla [I(r, z) \nabla \varphi(r, z)]$$



Linear approximation

$$\frac{\partial}{\partial z} I(r, z) \approx \frac{I(r, z_1) - I(r, z_2)}{2\Delta z}$$

$$\frac{I_1 - I_2}{I_1 + I_2} = -\frac{\Delta z}{k} \left[ \underbrace{\nabla^2 \varphi(r, z_0)}_{\text{Wave-front's curvature}} + \underbrace{\delta(e) \frac{\partial}{\partial n} \varphi(r, z_0)}_{\text{Wave-front's first derivative (Only on the signal's edge)}} \right]$$

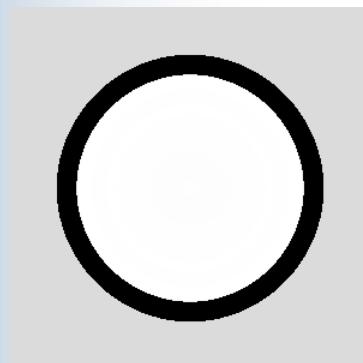
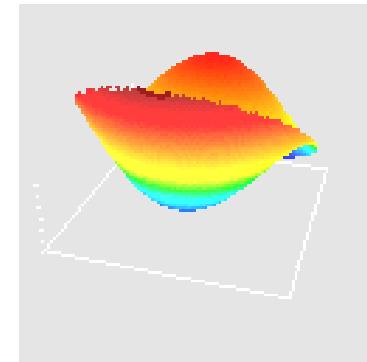
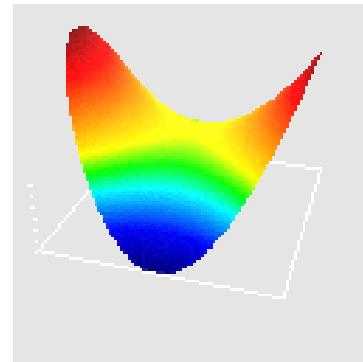
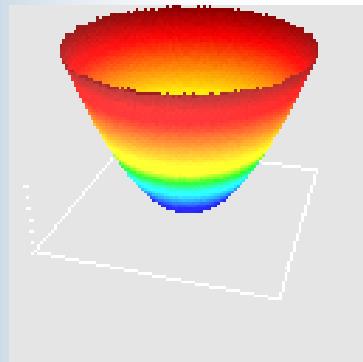
Contrast between  
images in two planes  
Sensor's signal ( $S$ )

Wave-front's  
curvature

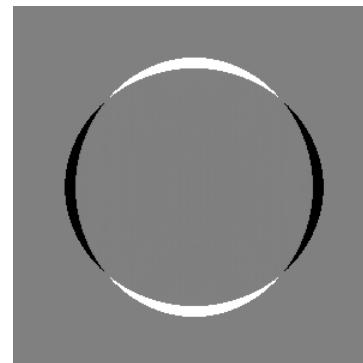
Wave-front's  
first derivative  
(Only on the signal's  
edge)

# Curvature sensing: a new method for ocular wave-front determination

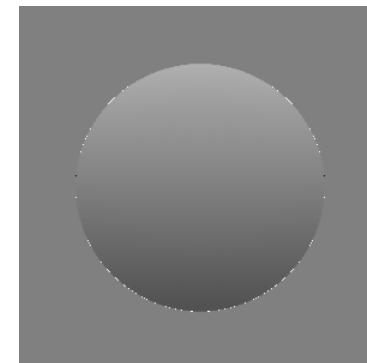
## Examples of S:



Defocus  
( $Z_2^0$ )



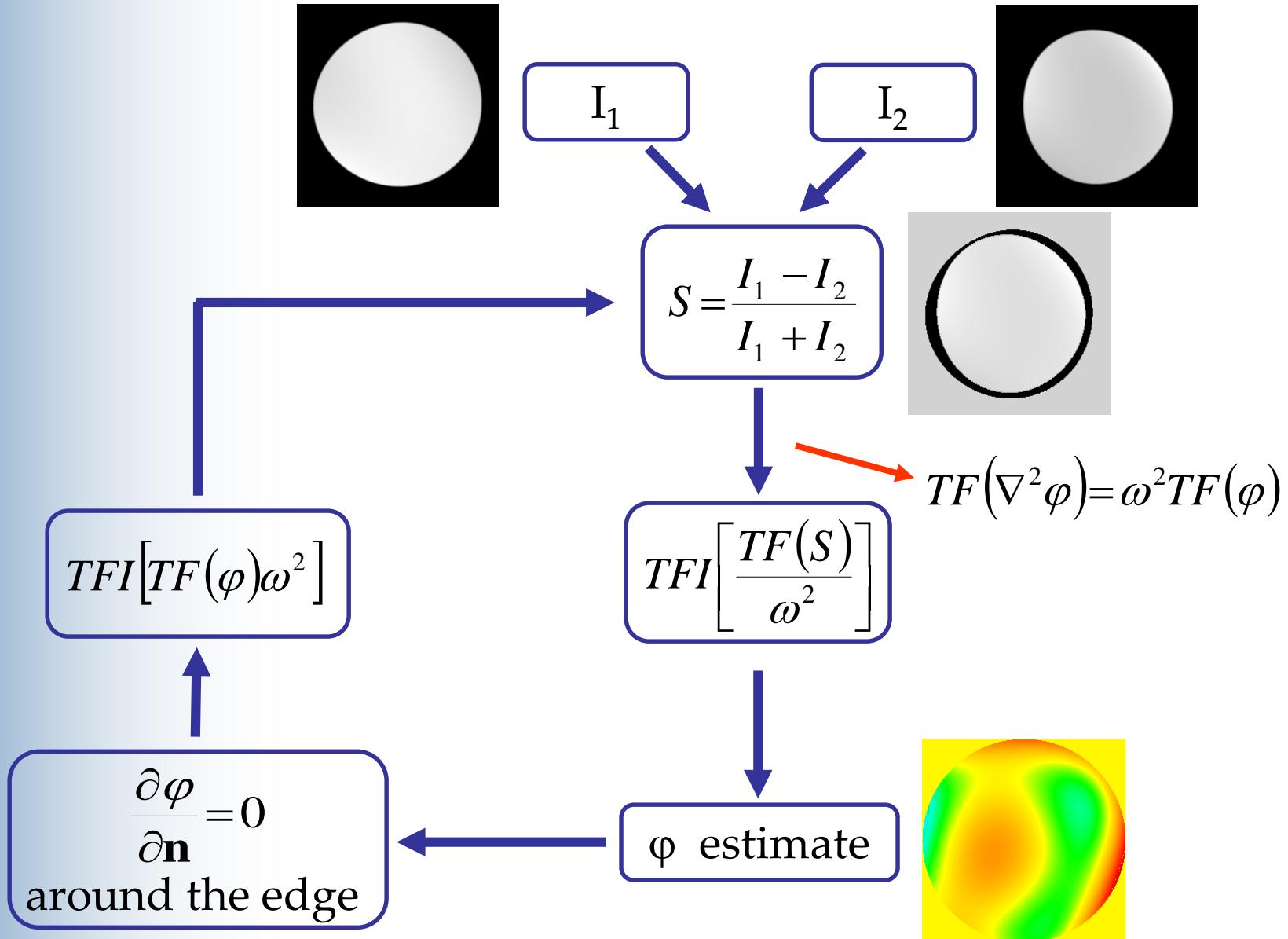
Astigmatism  
( $Z_2^2$ )



Coma  
( $Z_3^{-1}$ )

# Curvature sensing: a new method for ocular wave-front determination

## Iterative Fourier Transform algorithm



## Advantages:

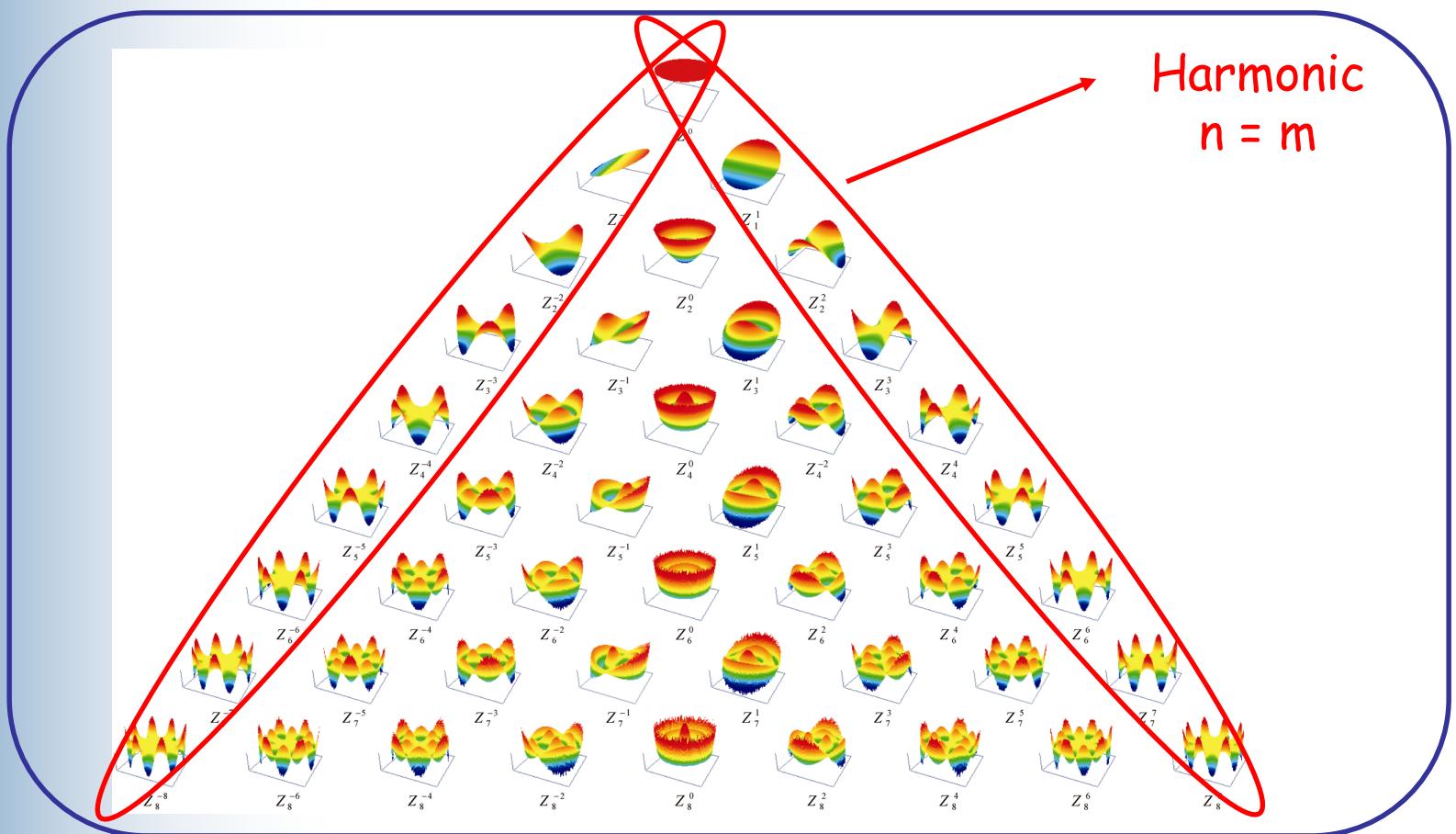
- A higher aberration order can be retrieved
- Much higher dynamic range for low order aberrations
- Is possible to retrieve information within pupil zones with reduced transmittance
- Application in very high frequency closed-loop adaptive optics systems
- Much cheaper

## Numerical simulations:

- Optimal placement of the detection planes
- Performance of the wave-front retrieval algorithm
- Optical system design
  - System's aberrations
  - Sensitivity
  - Dynamic range
- Noise

## Wave-front retrieval algorithm:

Problem: The second derivative is equal to zero for  
the harmonic modes

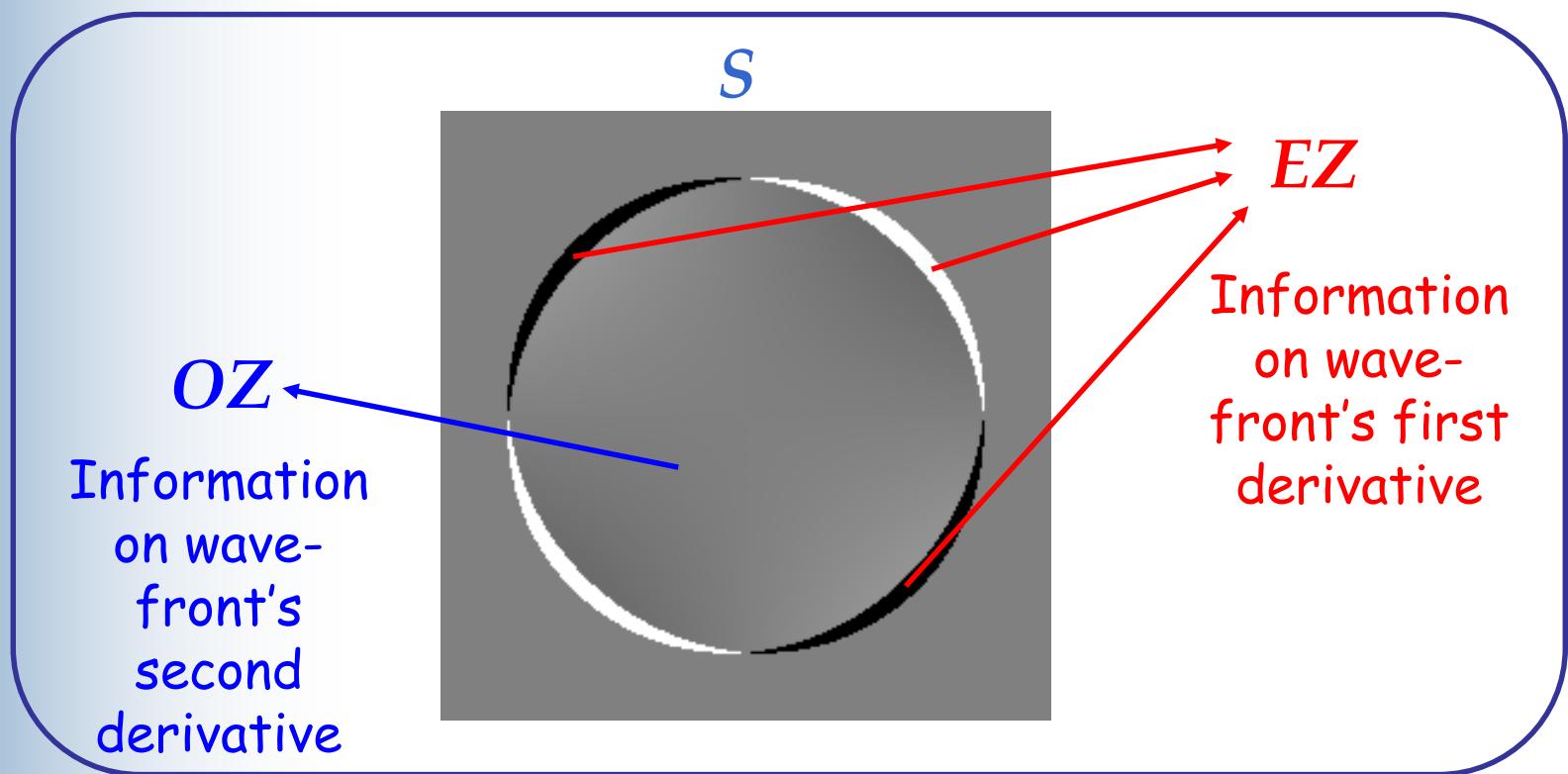


## Wave-front retrieval algorithm:

Classic solution: Imposing boundary conditions



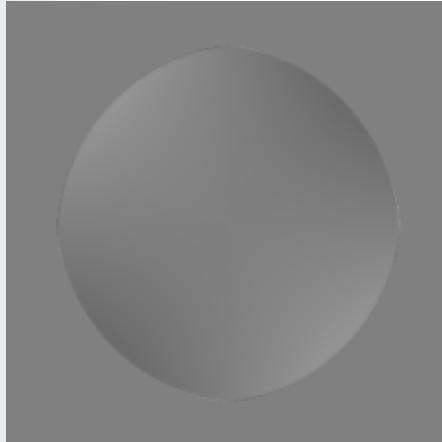
New solution: Separate the signal in two different zones  
and treat them independently



# Curvature sensing: a new method for ocular wave-front determination

## Wave-front retrieval algorithm:

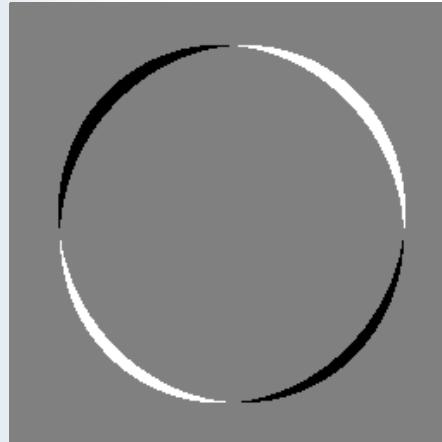
OZ



$$TFI \left[ \frac{TF(ZS)}{\omega^2} \right]$$

Contribution of  
non-harmonic  
modes

EZ

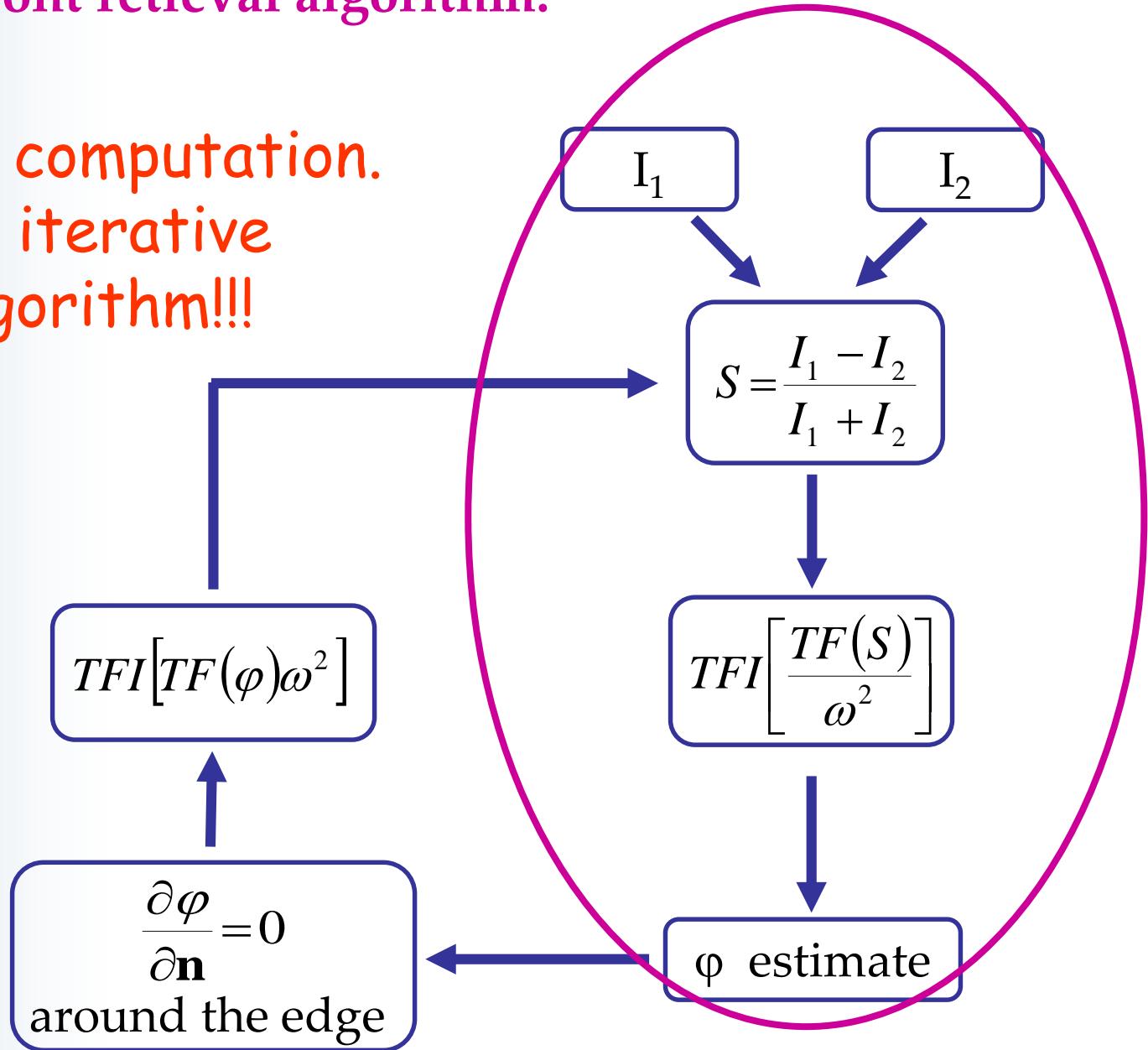


$$TFI \left[ \frac{TF(ZE)}{\omega^2} \right]$$

Contribution of  
harmonic modes

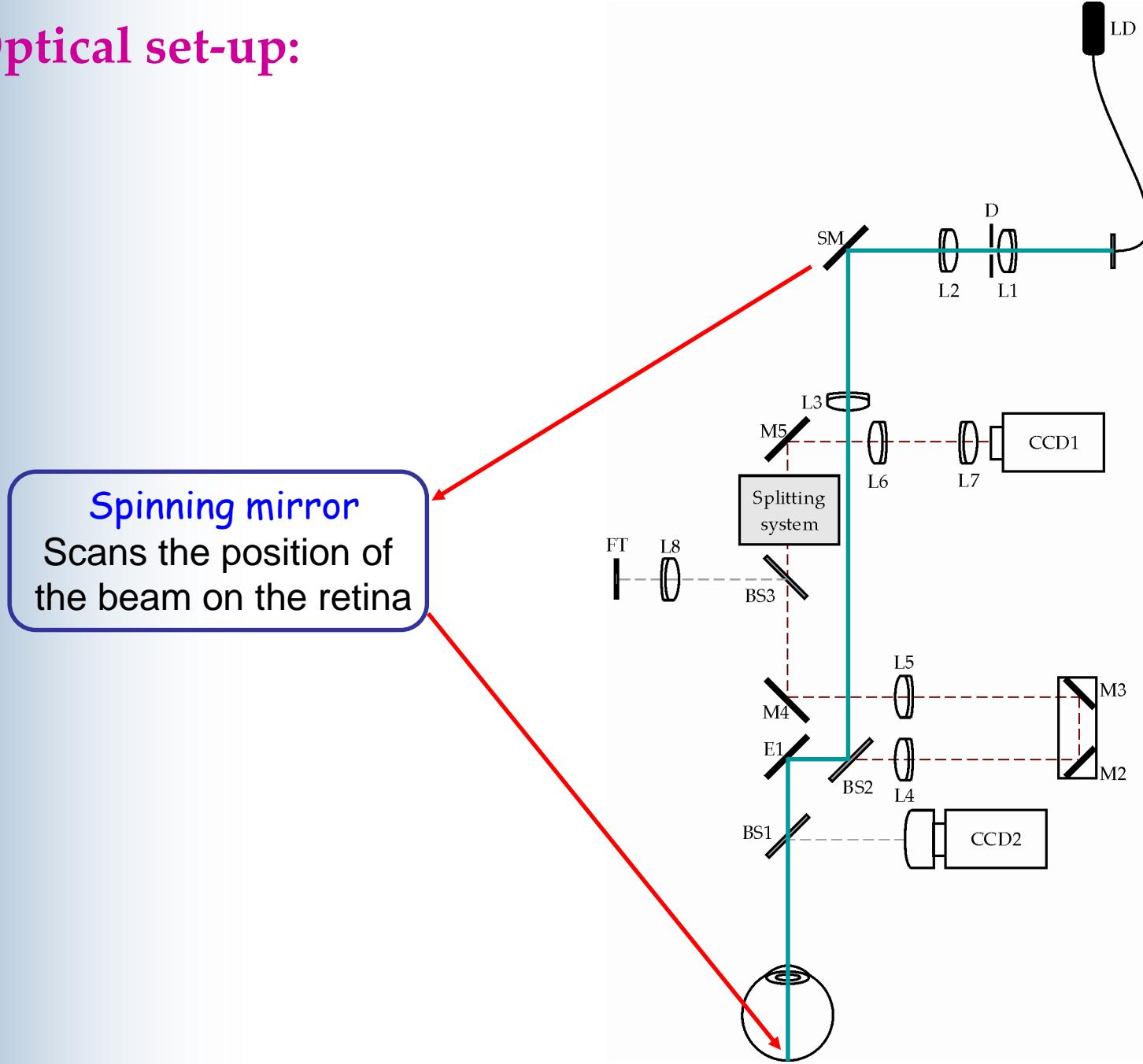
## Wave-front retrieval algorithm:

Direct computation.  
No iterative  
algorithm!!!



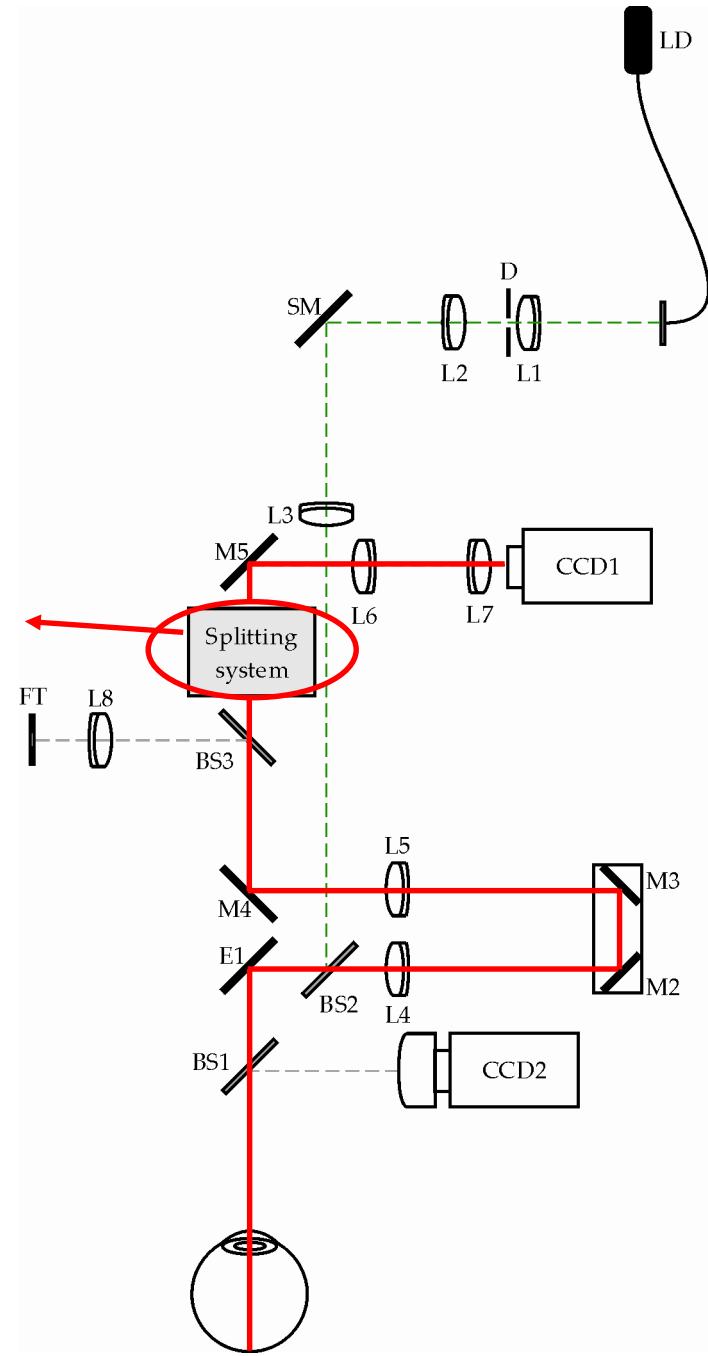
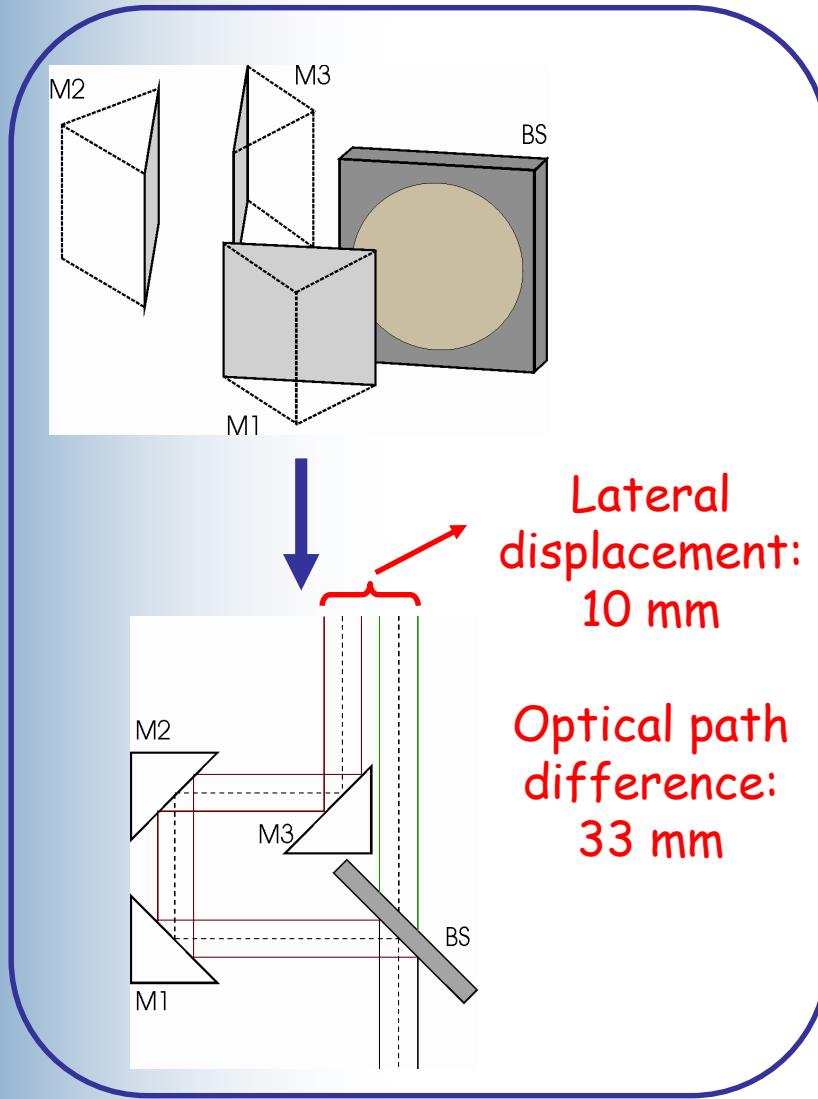
# Curvature sensing: a new method for ocular wave-front determination

## Optical set-up:



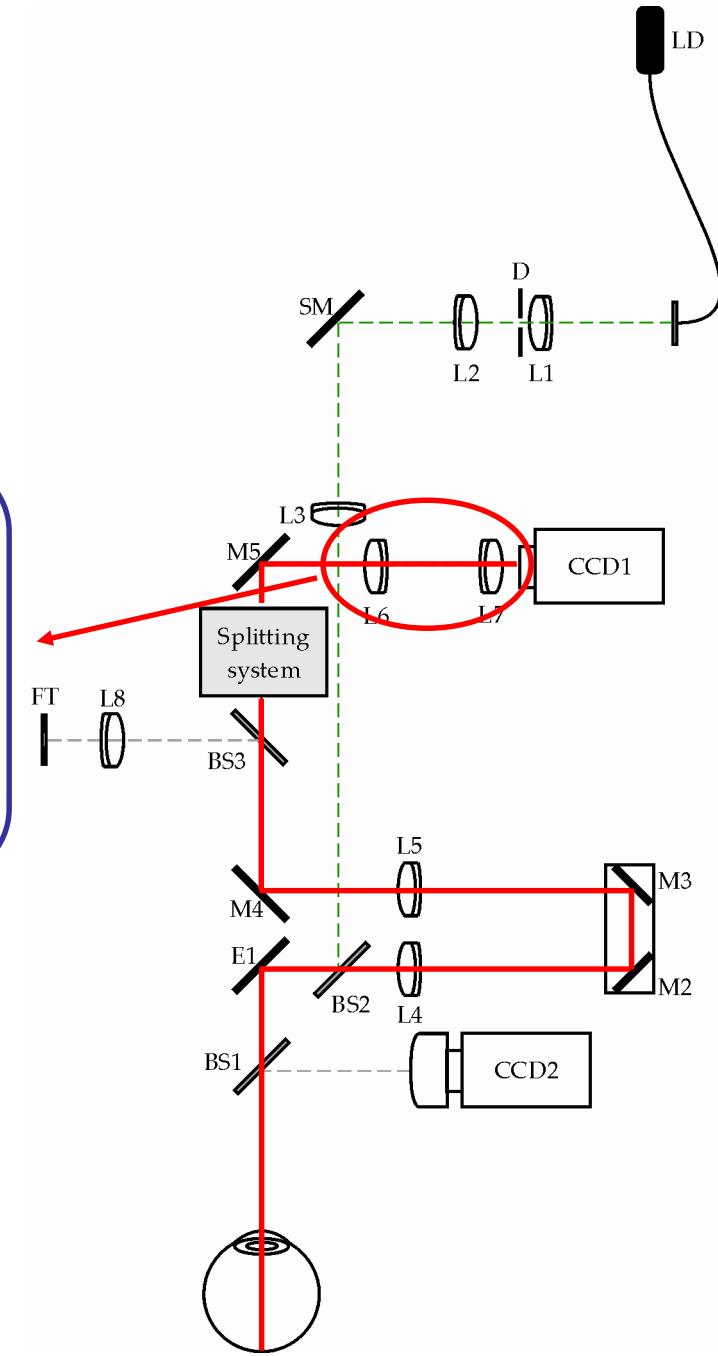
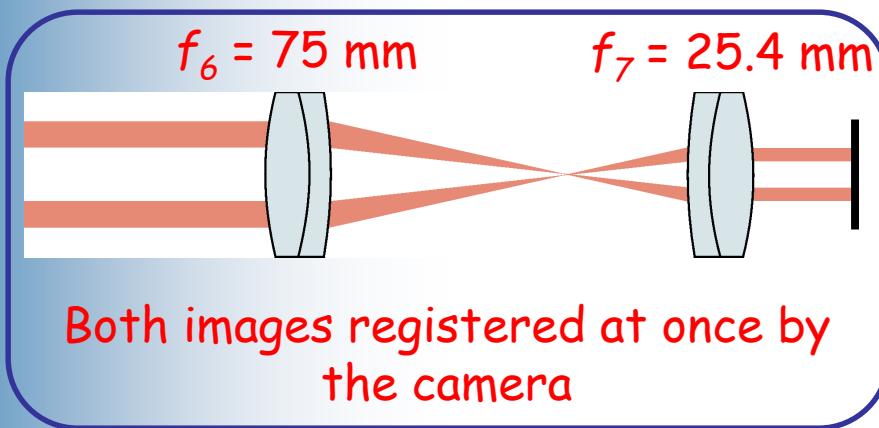
# Curvature sensing: a new method for ocular wave-front determination

## Optical set-up:



# Curvature sensing: a new method for ocular wave-front determination

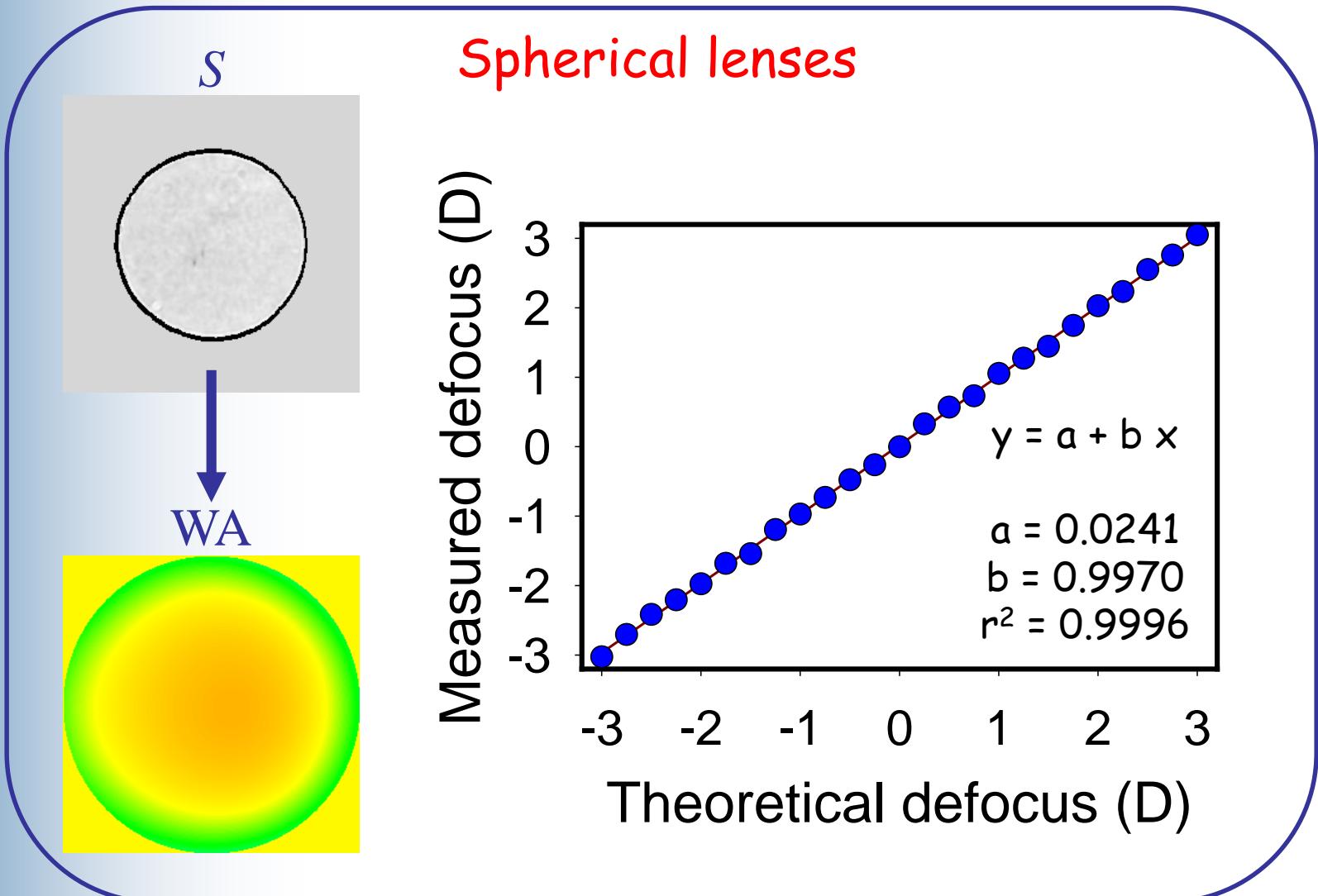
## Optical set-up:



# Curvature sensing: a new method for ocular wave-front determination

## Experimental results:

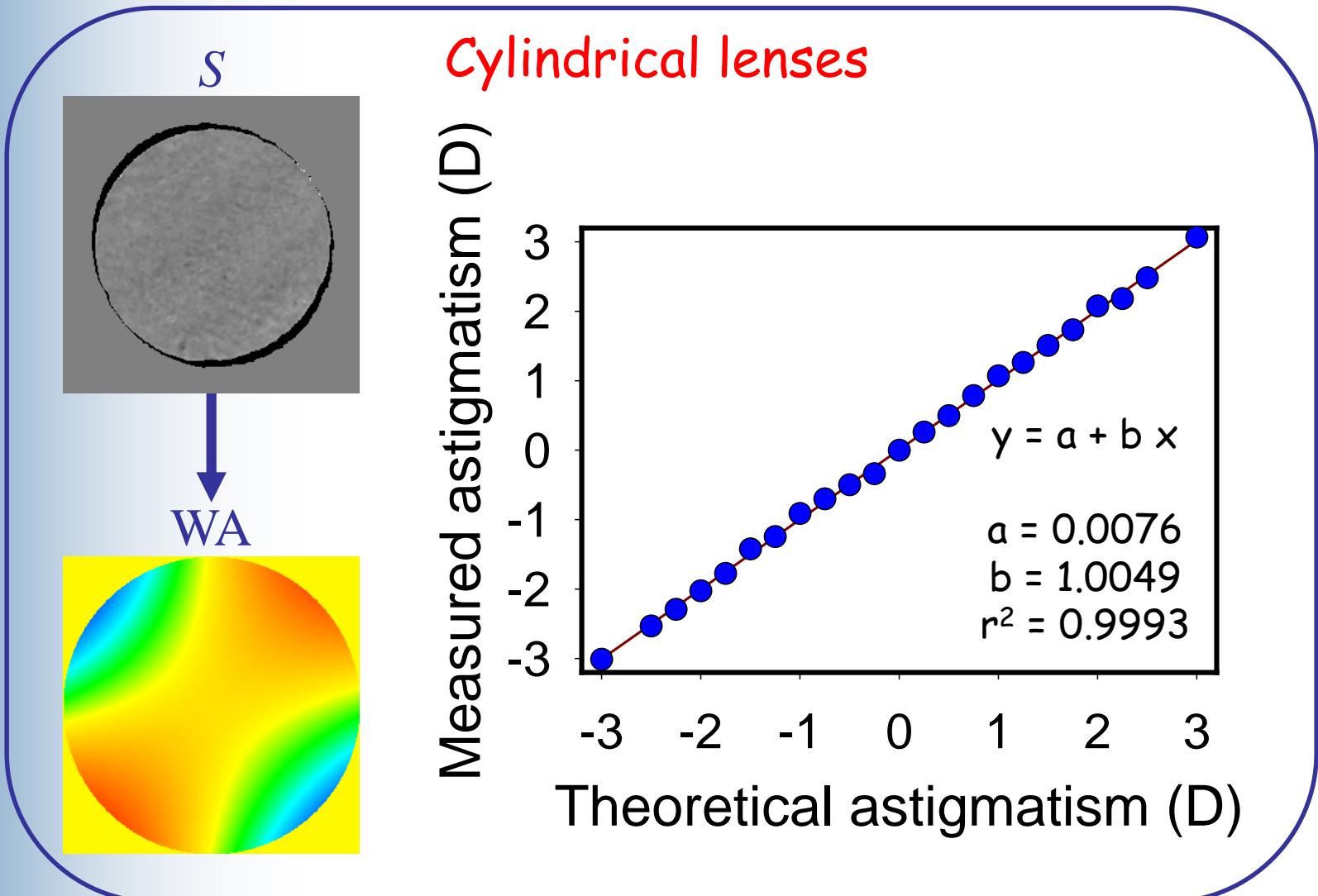
### Calibration:



# Curvature sensing: a new method for ocular wave-front determination

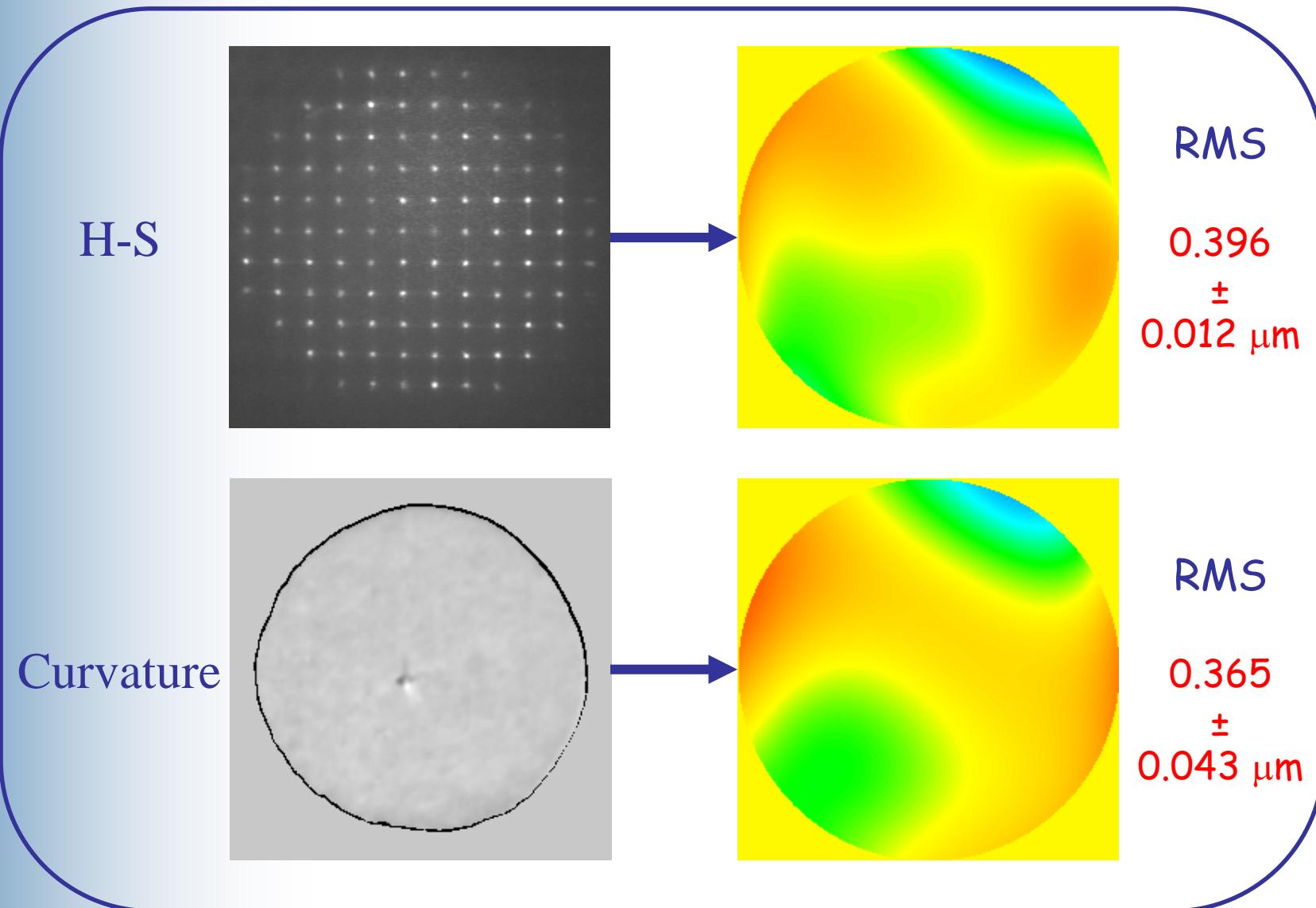
## Experimental results:

### Calibration:



# Curvature sensing: a new method for ocular wave-front determination

## Experimental results: Real eye's measurements:

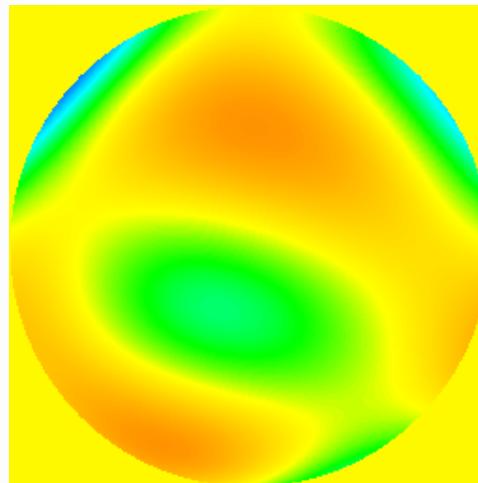


# Curvature sensing: a new method for ocular wave-front determination

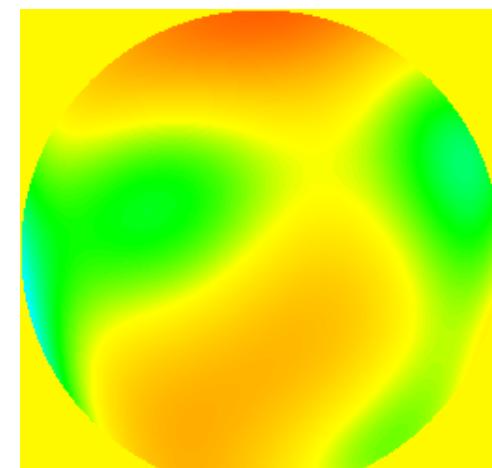
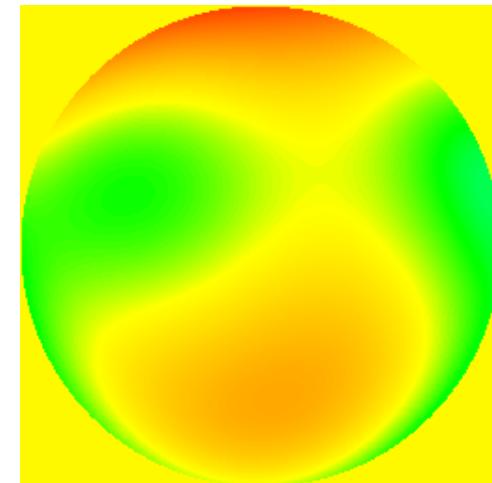
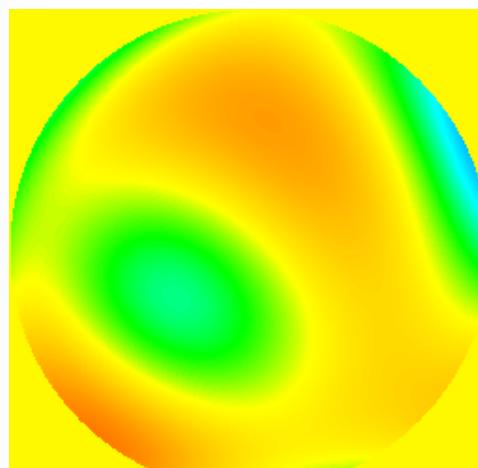
## Experimental results:

Real eye's measurements:

H-S



Curvature

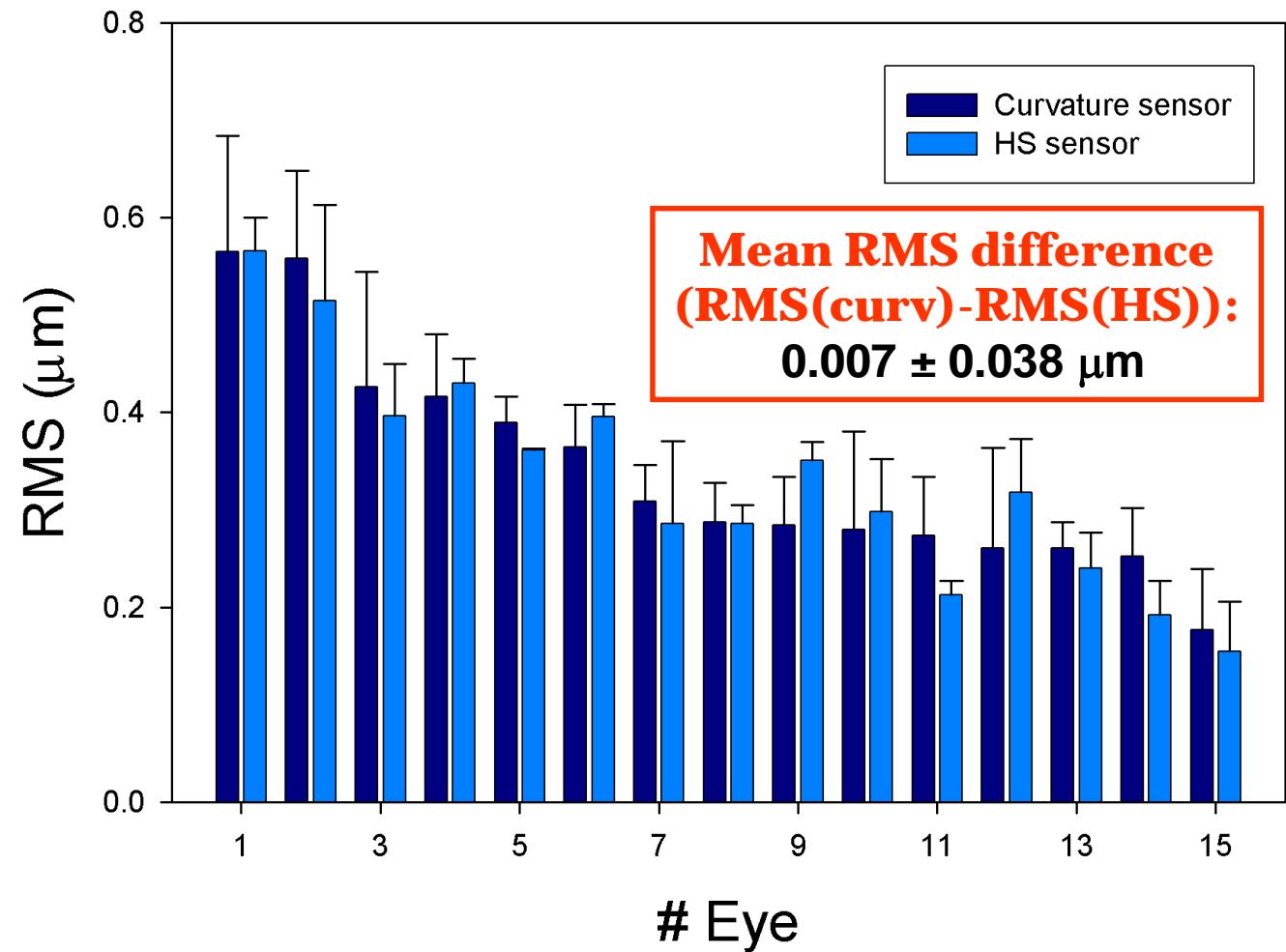


# Curvature sensing: a new method for ocular wave-front determination

## Experimental results:

Real eye's measurements:

N 15  
Mean age  $29.67 \pm 5.83$   
Mean refraction  $-1.27 \pm 1.85$



## Conclusions:

- We have implemented a curvature based wave-front sensor for ocular aberration determination.
- The performance of the system has been tested by means of numerical simulations, setting important parameters affecting the sensor's operation.
- The wave-front retrieval algorithm has been reformed. The new features make it faster with an increase in accuracy.
- Experimental measurements for both artificial and real eyes show results comparable to conventional sensors.
- Further work is needed to show the full potential of this technique.

Curvature sensing: a new method for  
ocular wave-front determination

Thank you  
for your  
attention!

Curvature sensing: a new method for  
ocular wave-front determination



**Centre de Desenvolupament de Sensors, Instrumentació i Sistemes**  
**Departament d'Òptica i Optometria**  
**UNIVERSITAT POLITÈCNICA DE CATALUNYA**



**CD6**



**TERRASSA**